



## ***CERT***

**Comité d'évaluation des  
ressources transfrontalières**

**Document de travail 2014/30**

Ne pas citer sans  
autorisation des auteurs

## ***TRAC***

**Transboundary Resources  
Assessment Committee**

**Working Paper 2014/30**

Not to be cited without  
permission of the authors

# **Estimation of the Intrinsic Rate of Increase for Georges Bank Yellowtail Flounder**

Loretta O'Brien and David McElroy  
NEFSC, Woods Hole, Ma

TRAC Georges Bank Yellowtail Flounder Diagnostic Benchmark  
April 14-18, 2014  
Woods Hole, Ma



# Introduction

- Estimate reproductive potential of GB yellowtail flounder using life-table analysis.
- Methodology based on the Euler-Lotka equation (Caswell 1989)
- Apply recently derived GB YT fecundity relationship that includes condition (WP 33)
- Analysis provides :
  - Intrinsic rate of increase  $\rightarrow r$  and instantaneous growth rate  $\lambda = \exp(r)$
  - Net Reproductive rate / reproductive potential  $\rightarrow R_0$

## Input Data:

- Time series : 1973-2013
- Population number at age (N); (2013 VPA ,Legault 2013)
- Recruitment (R) = age 1 N
- Sex ratio (X); assume 50/50
- Maturity at age (M); times series average (2013 VPA ,Legault 2013)
- Mean length at age =  $L_a$ 
  - Use NEFSC spring research bottom trawl survey : Closest to spawning time
  - Missing mean length for age 1 for most years, used a 10 year mean for missing years
  - Some missing age 6 or 7 , use average of adjacent years
  - Regression fit to observed mean length, fitted mean length applied in life-table

# Input Data:

- Condition

- Individual weight only available since 1992.
- Fulton’s Condition at length (l) =  $K_l = [Wt (g) / Length (mm)^3 ] * 100000$
- K assumed = 1 for earlier years
- Mean K at age =  $K_a = \Sigma (K_l / n)$
- Potential Annual Fecundity (F) : combined 2010-2013 (WP 33 McElroy )
  - $\ln (PAF)_a = \beta_0 + \beta_1 \ln L_a (mm) + \beta_2 \text{Oocyte diam} + \beta_3 K_a$
  - oocyte diameter = 450 um (near spawning size)

Parameter	Estimate	SE
Intercept	-3.3816805	2.7745847
LN (TL)	2.6875112	0.4542765
Mean Oocyte Diameter	-0.0023884	0.0005946
K	2.8512876	0.2466295

- Total Egg production at age =  $TEP_a = N_a * X_a * M_a * F_a$

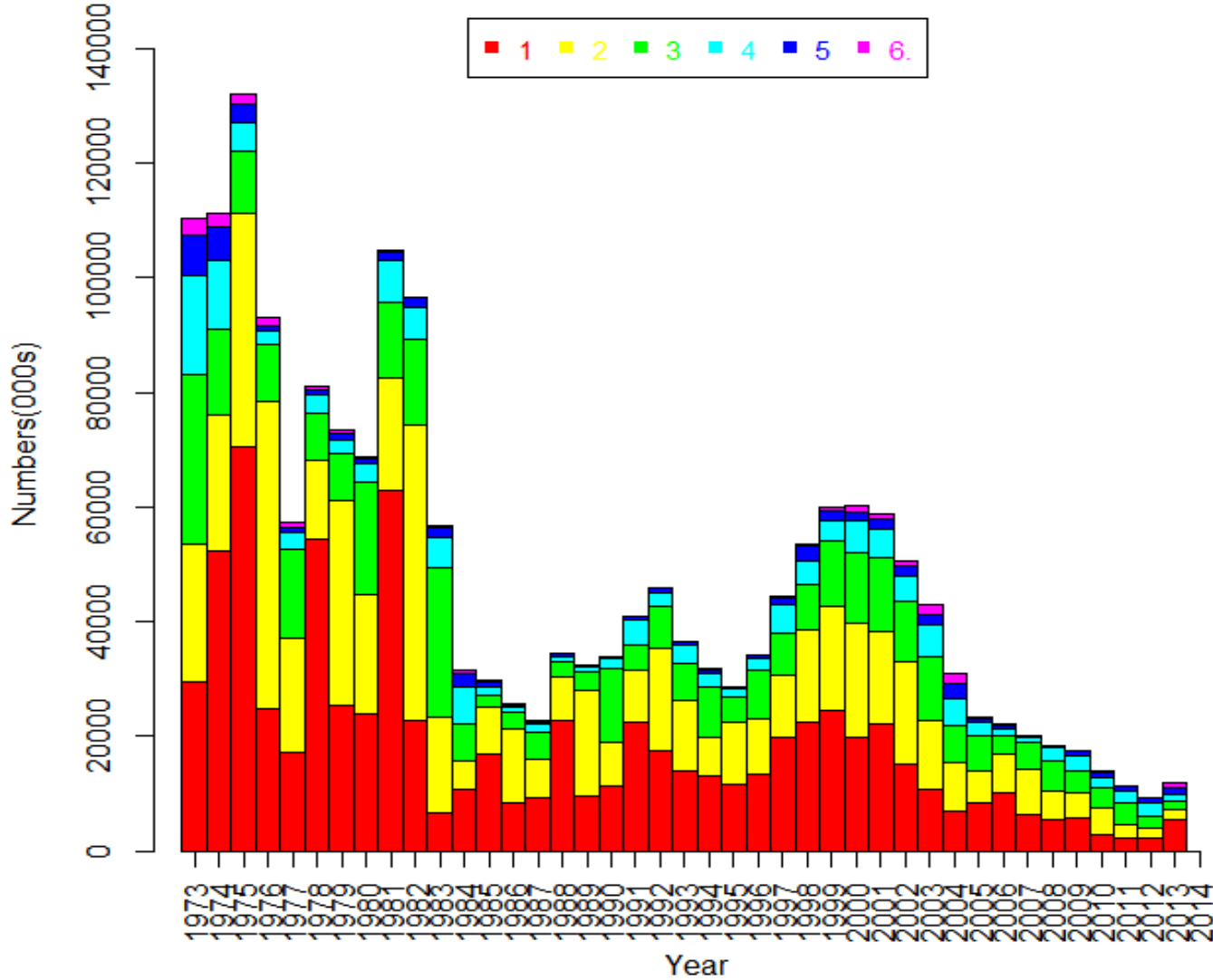
- Recruitment survival =  $S = R_{y-1} / TEP_y$

- Average Rct Z =  $( \Sigma -\ln [R/TEP]_y ) / n$

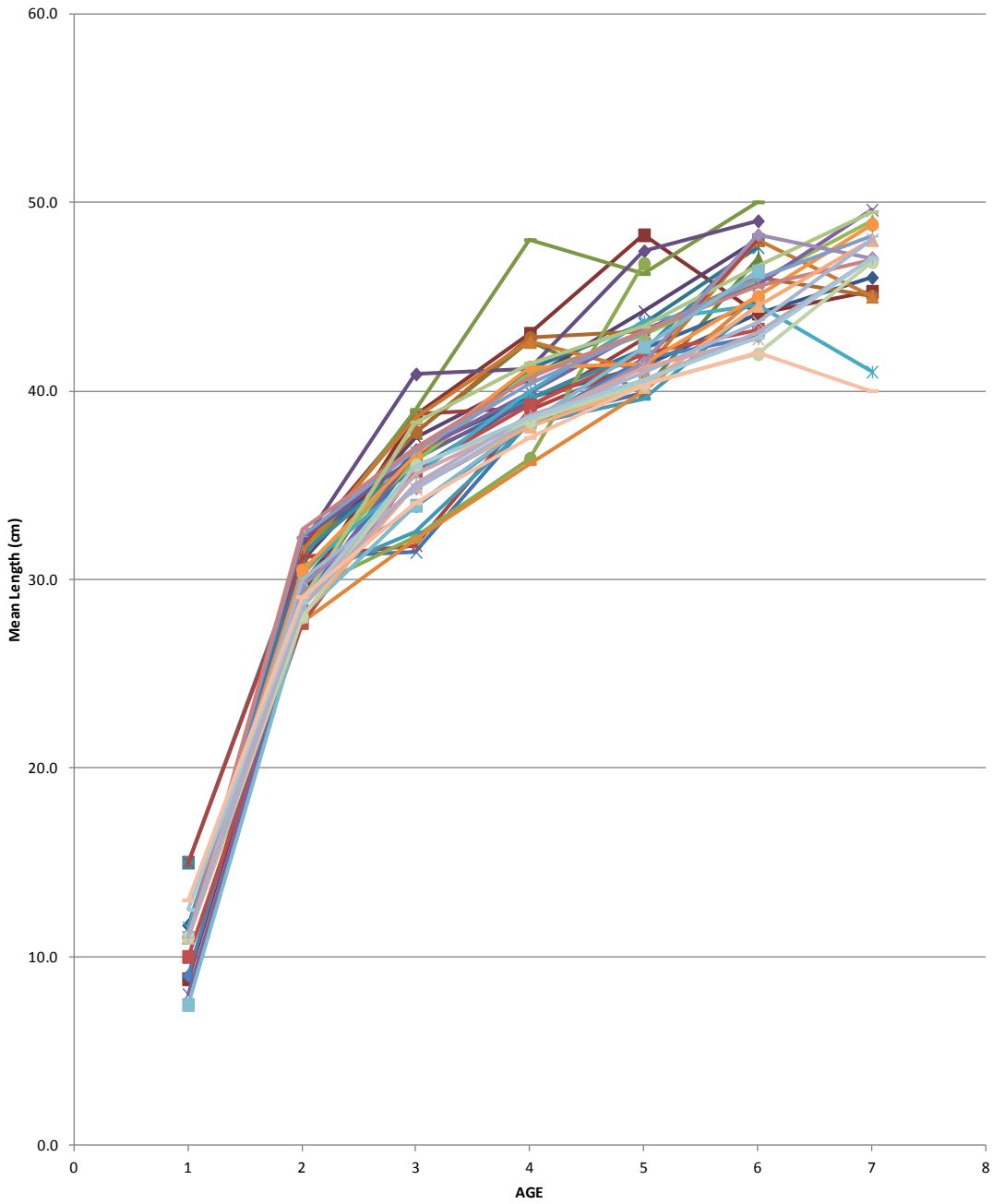
- Maximum age ~ 11

# Population Numbers at ages 1-6+ from 1973-2013

## Georges Bank Yellowtail Flounder

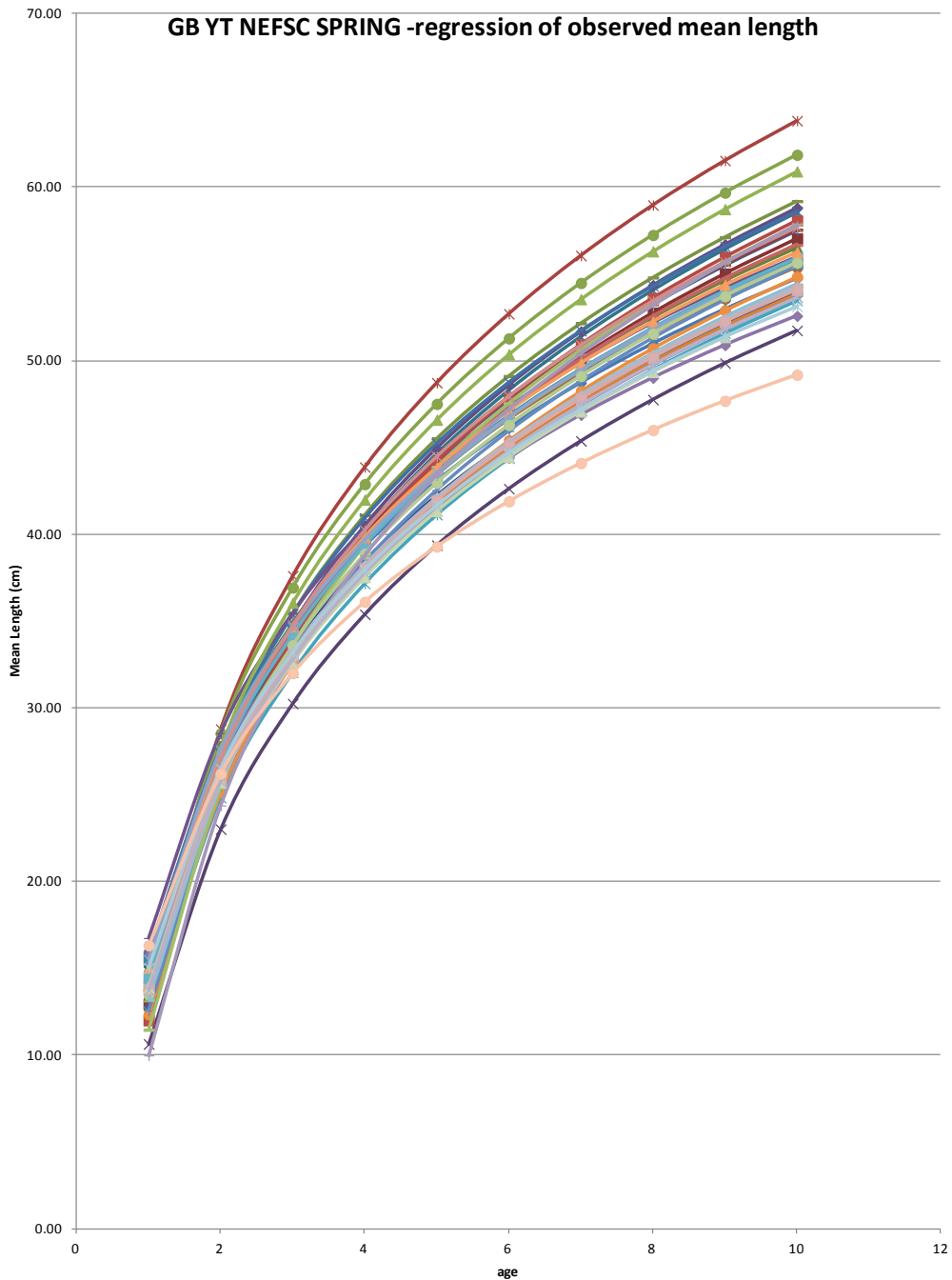


### GB YT NEFSC Spring - Observed Mean Length



**Spring  
Observed  
Mean length at age  
1973-2013**

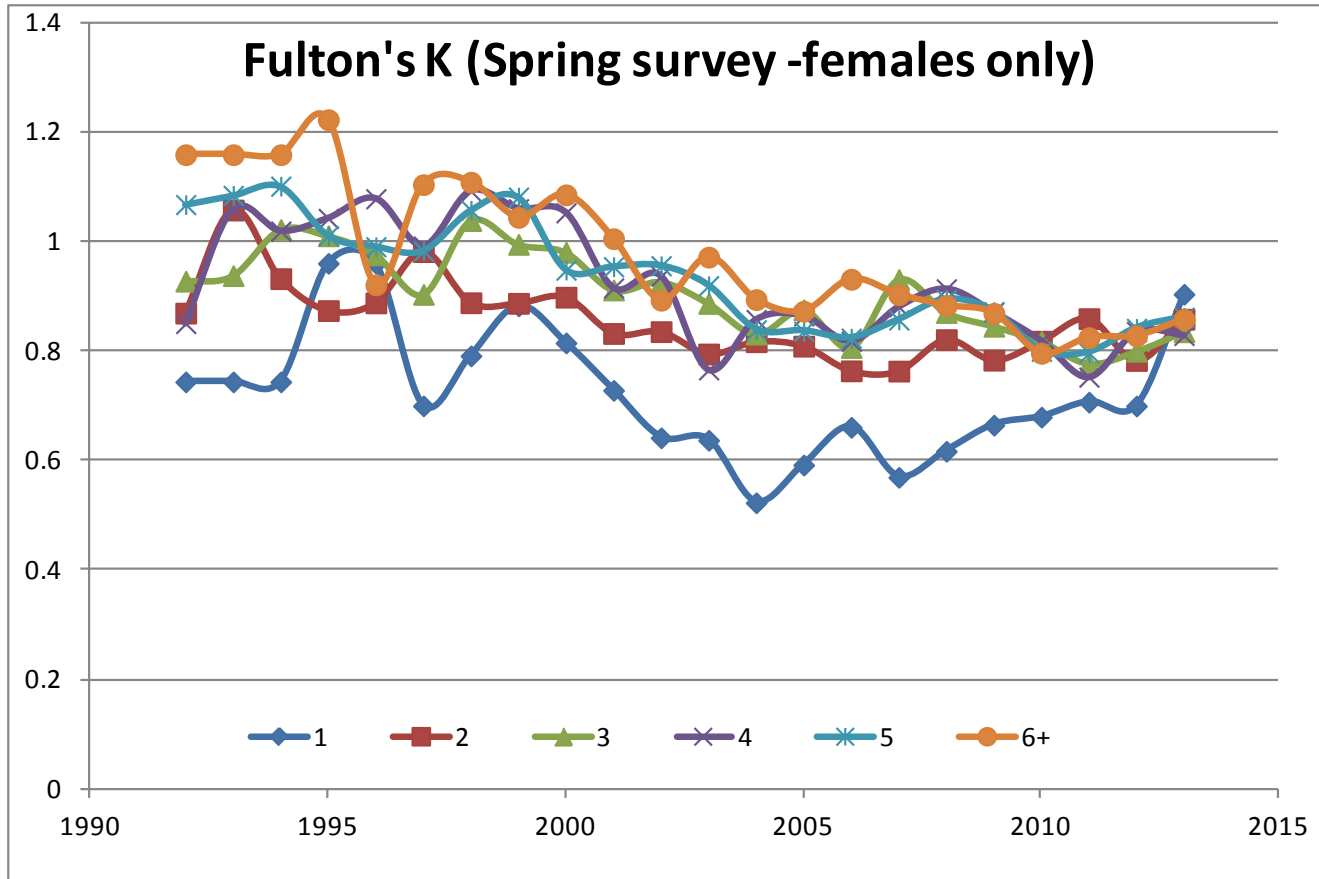
### GB YT NEFSC SPRING -regression of observed mean length



Spring  
Fitted mean length at age  
1973-2013

Ages 7+ low sample size

# Fulton's Condition





# Life-Table Analysis

Euler-Lotka equation ; solve to estimate  $r$ , intrinsic rate of increase

$$\sum_{x=\alpha}^{x=\beta} e^{-rx} l(x) m(x) = 1$$

where

- $l(x)$  = the probability of surviving to age  $x$
- $m(x)$  = number of female offspring produced at age  $x$
- $\alpha$  = age 0
- $\beta$  = maximum age

Derive annual instantaneous growth rate :

- $\lambda = \exp(r)$

# Life-Table Analysis

Derive Net reproductive rate:

$$R_o = \sum_{x=\alpha}^{x=\beta} l(x) m(x)$$

where

$l(x)$  = the probability of surviving to age  $x$

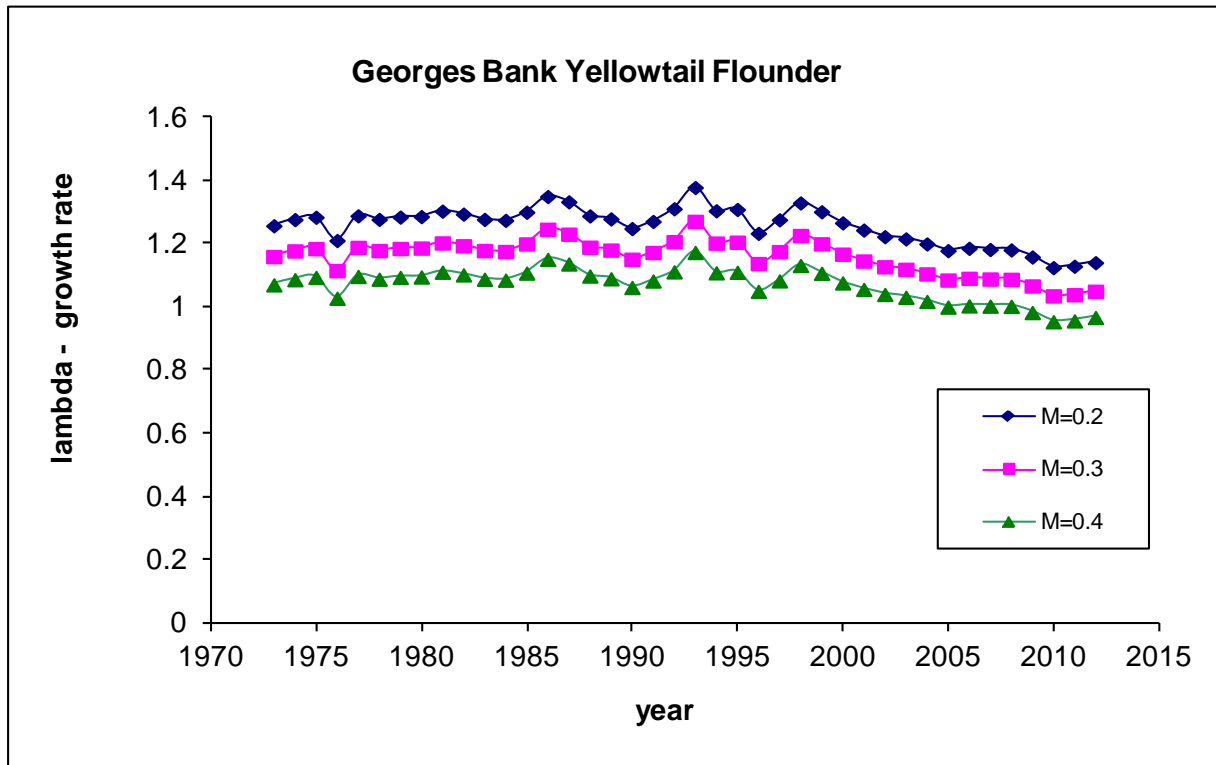
$m(x)$  = number of female offspring produced at age  $x$

$\alpha$  = age at maturity

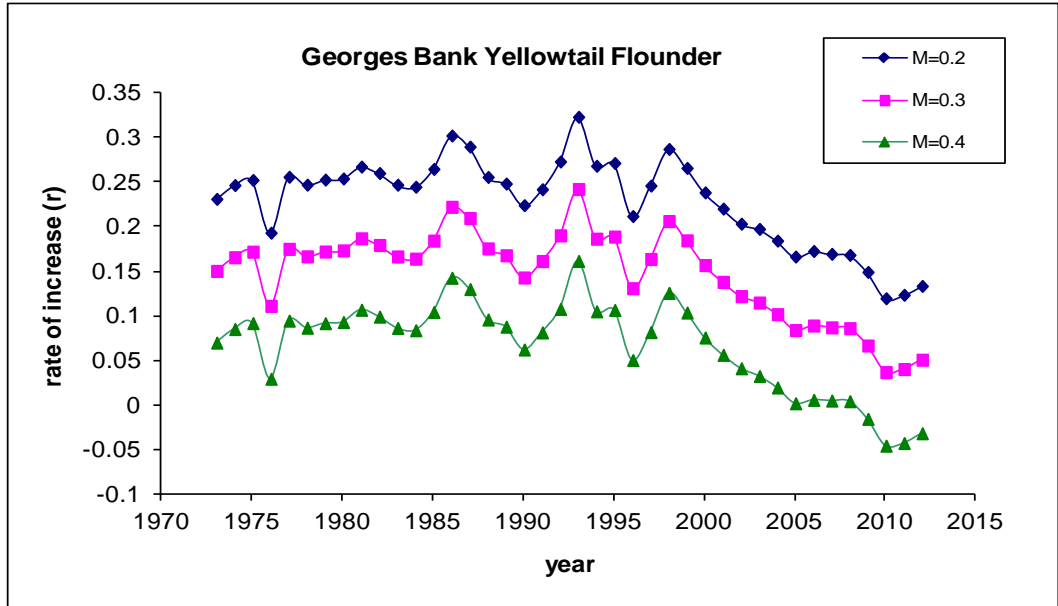
$\beta$  = age at death

# Results

annual instantaneous growth rate :  $\lambda = \exp(r)$

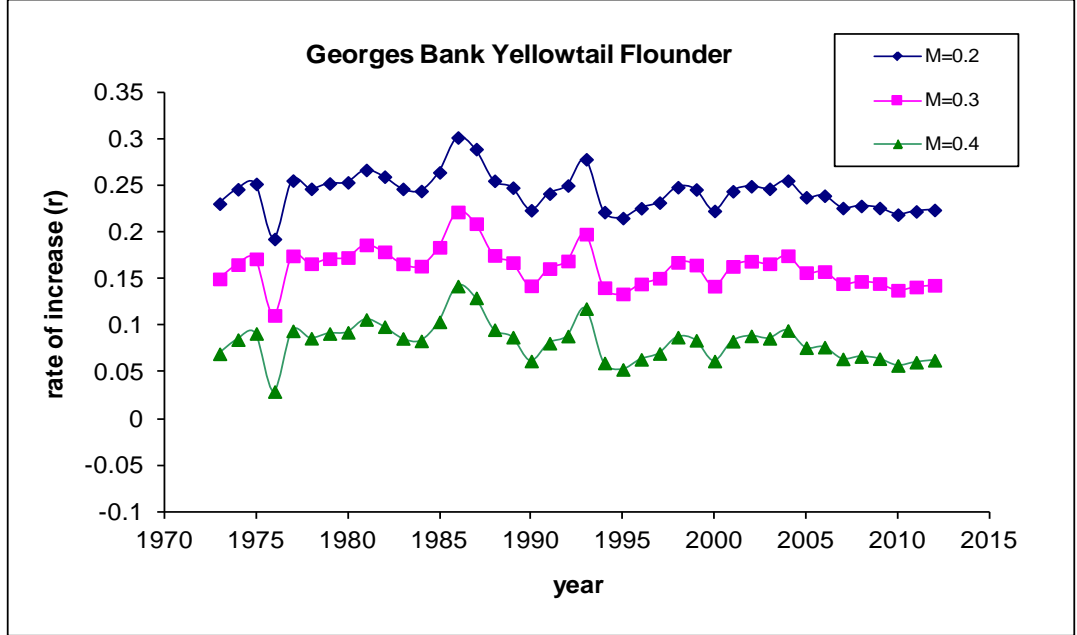


# Results – influence of K on r



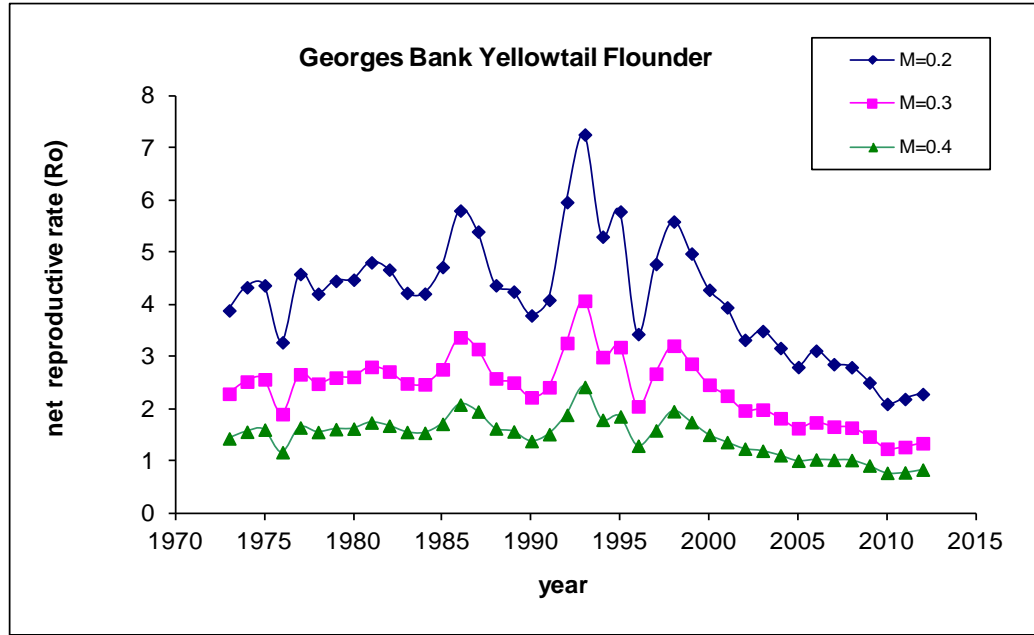
K has strong effect on trend in r

K = 1 in fecundity eqn from 1973-1991  
K = observed condition from 1992 →



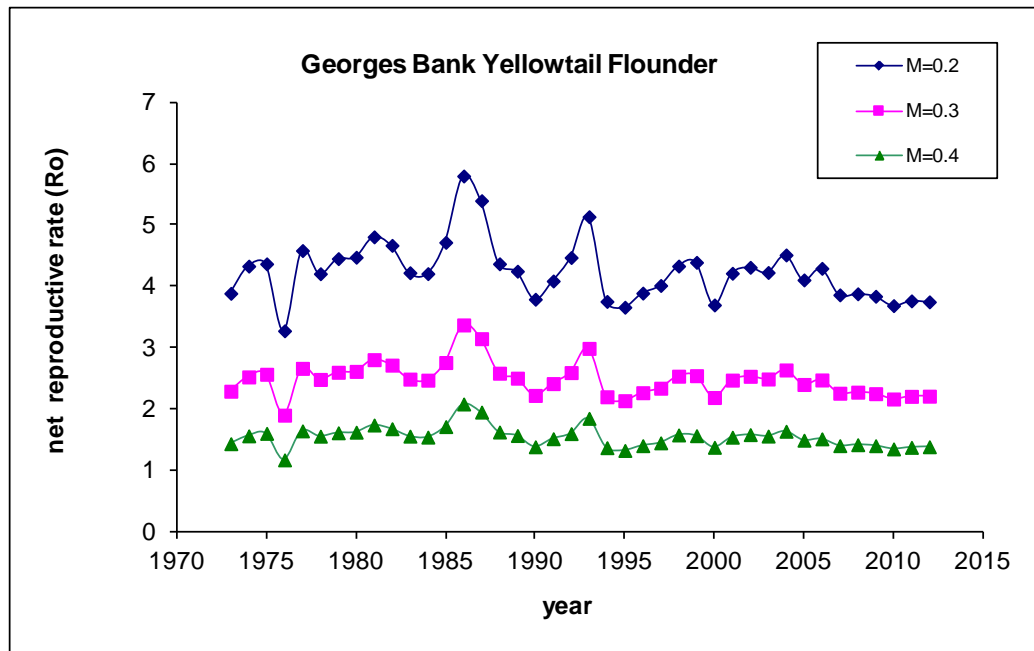
K = 1 in all years

# Results – influence of K on Ro



K has strong effect on trend in  $R_o$

K = 1 in fecundity eqn from 1973-1991  
K = observed condition from 1992 →



K = 1 in all years

# Summary

- Population growth ( $\lambda$ ) and net reproduction ( $R_0$ ) have been declining since 1998
- Estimation of  $r$  and  $R_0$  influenced strongly by inclusion of condition in fecundity estimation
- If condition is not included, would mistakenly conclude stock is relatively stable even though population numbers are declining.

## Further work:

- Sensitivities to varied sex ratio, since YT have dimorphic growth; Females grow/survive to larger size than males
- Sensitivity and Elasticity (proportional effect) to measure how changes in vital rates i.e. juvenile mortality, survival at age, effect estimation of  $\lambda$
- Projections of Spawning Stock Biomass (Monte Carlo Analysis)

# Literature Cited

Caswell, H. 1989. Matrix Population Models. Construction, Analysis, and Interpretation. Sinauer Associates, Inc. Sunderland , Ma. 328 p.

Hood, G. M. (2011) PopTools version 3.2.5. URL <http://www.poptools.org>

McElroy, W.D., E.T. Towle, M.J. Wuenschel, and R.S. McBride. 2013. Spatial and annual variation in fecundity of yellowtail flounder in U.S. waters. TRAC GBYT Benchmark WP33

Legault, C. 2013. Stock Assessment of Georges Bank Yellowtail Flounder for 2013. TRAC 2013 WP . 138 p.