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# An Assessment of the Northwest Atlantic Mackerel (Scomber scombrus L.) with XSA (Extended Survivors Analysis) 

François Grégoire ${ }^{1}$ and Jean-Jacques Maguire ${ }^{2}$
${ }^{1}$ Fisheries and Aquaculture Science Branch Department of Fisheries and Oceans Canada

Maurice Lamontagne Institute
850 Route de la Mer
Mont-Joli, Qc
G5H 3Z4
Canada
${ }^{2} 1450$ Godefroy Québec, Qc
G1T 2E4
Canada

## Canadä

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#### Abstract

The abundance of Northwest Atlantic mackerel (Scomber scombrus L.) was evaluated using extended survivors analysis (XSA). The selected formulations have all presented adjustment problems that could be explained by a conflict between the catch at age and abundance index data. Despite these problems, the results were similar to those produced by analysis methods that do not require an abundance index. All these results suggest that current data describing the demographic structure and measuring the Atlantic mackerel abundance are not consistent with traditional methods of analytical assessment.


#### Abstract

RÉSUMÉ

L'abondance du maquereau bleu (Scomber scombrus L.) du Nord-Ouest de l'Atlantique a été évaluée à l'aide de l'analyse étendue des survivants (XSA). Les formulations retenues ont toutes présenté des problèmes d'ajustement qui pourraient s'expliquer par un conflit entre les données de la capture à l'âge et celles de l'indice d'abondance. Malgré ces problèmes, les résultats obtenus se sont avérés semblables à ceux produits par des méthodes d'analyse n'utilisant pas d'indice d'abondance. Tous ces résultats portent à croire que les données actuelles décrivant la structure démographique et mesurant l'abondance du maquereau bleu ne se prêtent pas bien aux méthodes traditionnelles d'évaluation analytique.


## INTRODUCTION

The abundance of Northwest Atlantic mackerel (Scomber scombrus L.) was evaluated in March 2010 by the Transboundary Resources Assessment Committee (TRAC). Various analytical models were presented during this assessment as well as different formulations of the same model. A first model, the separable VPA (Pope and Shepherd 1982), was carried out using only the catch at age. A second model, the traditional VPA (Darby and Flatman 1994), was run with abundance and fishing mortalities data from the separable VPA. The results of these models were described and compared in Grégoire and Maguire (2011).

The objective of this document is to present the results of an assessment conducted using a third analytical model, the extended survivors analysis (XSA). Unlike the separable VPA, XSA requires the input of one or several abundance indices.

## MATERIAL AND METHODS

## XSA

The extended survivors analysis (Shepherd 1992, 1999) is an extension of the survival analysis developed by Doubleday (1976, 1981). Compared to the latter, XSA allows the use of several abundance indices from scientific surveys and/or catch per unit effort from the commercial fishery. XSA is widely used by ICES for groundfish assessments. As part of this study, different formulations were tested using the VPA software, version 3.2 (Darby and Flatman 1994).

## Data Input

The assessment by XSA covered the period 1962-2008. For each formulation tested, the input data were: (1) catch ('000) at age, (2) catch weight (kg) at age, (3) population weight (kg) at age based on the Rivard method (NOAA Fisheries Toolbox 2009a), and (4) maturity at age (Canadian data). Natural mortality was set at 0.2 for all years and ages, and the proportions of natural and fishing mortality before spawning at 0.5 .

## Index of Abundance

XSA was calibrated using an index of abundance from a spring bottom trawl survey (Dr. Gary Shepherd and Dr. Jon Deroba, NOAA Fisheries, pers. com.). Mean catch per set in numbers and weight were presented as well as mean numbers per set at age. The year-classes were described as the proportion of young age groups (ages 1-3 and ages 1-4). The follow-up of the year-classes in the survey was realized by comparing the abundance of adjacent age groups (i.e. ages 1-2, ages 2-3, etc...).

The instantaneous rates of total mortality $(Z)$ were calculated from the relationship between the catches per set from several age groups for consecutive years. For example, the $Z$ estimate for 2007 for the age groups $4^{+}$and $5^{+}$was calculated as follows:

$$
\ln \left(\sum \text { age } 4^{+} \text {for } 2007 / \sum \text { age } 5^{+} \text {for } 2008\right)
$$

The instantaneous rates of total mortality were also calculated based on the Sinclair (1998) method for blocks of 4 and 5 years and for age groups 2-6, 3-7 and 4-8. Supposing a constant natural mortality, the $Z$ obtained with this method represent an estimate of fishing mortalities.

## XSA Runs

## Exploratory

Several formulations were tested by varying the study period, the total number of years and type of relationships used to weight the older data, the selected age groups ( $1-6^{+}, 1-7^{+}$, etc), the abundance index used overall or split, and ages at which catchability is considered fixed and independent of population size.

## Final

The final formulations were selected based on the examination of residuals, the residual means squared (the smallest value) and the standard errors of catchability estimates. For a given age, a standard error greater than 0.5 (log scale) indicates a problem in the quality of the corresponding index (Darby and Flatman 1994). The regression slopes used to calculate catchability were tested to see if they were significantly different from the unit. In the event of a significant difference, the corresponding catchabilities were considered as proportional to abundance (Darby and Flatman 1994).

The final choice fell on two formulations (Run 1 and Run 2) producing identical results and diagnoses. What differs from these formulations involve the characteristics attributed to catchability, namely: (1) the age groups for which catchability is independent of abundance, and (2) the age groups from which catchability is constant.

By comparison, a third formulation (Run 3) was chosen, taking into account that age groups one to six, the latter being a "real" age group rather than a $6^{+}$made up of all fish of age six and over.

## Constant Catchability

The first formulation (Run 1) chosen was used to test the hypothesis that catchability coefficients have not changed over the years. To do this, and as proposed by Mohn (1999), several XSA models were produced for different periods of years.

## References Points

## Yield Per Recruit Analysis

The reference points associated with fishing mortality were calculated using a yield per recruit analysis (YPR) (NOAA Fisheries Toolbox 2009b). The input data for this analysis are the averages (2004-2008) of the following parameters: (1) partial recruitment at age (selectivity) calculated from fishing mortalities (ages 3-5, weighted by the corresponding abundances) from the second model chosen (Run 2), (2) natural mortality set at 0.2 for all years and all age groups, (3) catch weight (kg) at age, (4) population weight (kg) at age based on the Rivard method (NOAA Fisheries Toolbox 2009a), and (5) maturity at age (Canadian data). The reference points calculated by this analysis are $F_{0.1}, F_{\text {max }}$, and $F$ at $40 \%$, the latter being considered by the Northeast Fisheries Science Center as a proxy of $F_{m s y}$. This analysis also calculated the ratio between spawning stock biomass and recruitment (SSB/R).

## Deterministic Calculations of MSY and SSB $_{\text {msy }}$

For the second formulation chosen (Run 2), in which the residual mean squared was slightly lower than the first formulation (Run 1), the maximum sustainable yield, or MSY, was obtained analytically from the product of yield per recruit (Y/R) at $F_{\text {msy }}$ ( $F$ at $40 \%$ ) and recruitment (average historical level). Spawning stock biomass at maximum sustainable yield or $\mathrm{SSB}_{\text {msy }}$ was obtained by the product between the value of SSB/R at $F_{\text {msy }}$ and recruitment (average historical level). The status of the population for 2008 was described with the following ratios: (1) fishing mortality (ages $3-5$, averages weighted by the corresponding abundances) in 2008 and $\mathrm{F}_{\text {msy }}$, and (2) spawning stock biomass in 2008 and SSB $_{\text {msy }}$.

## Stochastic Calculations of MSY and SSB msy $^{\text {M }}$

The MSY and SSB $_{\text {msy }}$ reference points were also calculated using the AGEPRO procedure (NOAA Fisheries Toolbox 2009c). In addition to the parameters used in the yield per recruit analysis, AGEPRO requires as input recruits (age one) and abundance at age from the XSA results. The empirical cumulative distribution (ECD) (Model 14) was selected as the model describing the recruitment and spawning stock biomass relationship rather than a model whose form is already predetermined such as the Beverton-Holt (Model 5) and Ricker models (model 6). The ECD model generates recruitment values, assuming that their distribution is stationary and independent of stock size.

Projections were calculated with a 100-year outlook with $\mathrm{F}_{\text {msy }}$ as the annual harvest strategy. After a rapid increase, SSB $_{\text {msy }}$ and MSY values stabilized after some years. The selected values represent the averages for the 2020-2108 period.

## RESULTS

## Abundance Index

Beginning in the late 1980s, mean numbers and weight per set gradually increased to peak in the 2000s (Table 1, Figure 1). Some of the strong year-classes observed in the commercial fishery over several years (Grégoire and Maguire 2011), such as 1967 and 1999, almost disappeared from the survey after only a few years (Table 2, Figure 2). At age one, the strong year-classes of 1974, 1982, 1988 and 1996 were virtually absent from the survey (Figure 3A) as was 1967, 1974, 1982, 1988, 1996 and 2003 at age two (Figure 3B). The late 1990s and the 2000s were mainly characterized by the presence of younger age groups (Figure 2). In fact, over $95 \%$ of catches in the survey since 1997 were composed of individuals of age 4 or younger (Figure 4A), and over 90\% of age 3 or younger (Figure 4B).

Several year-classes have not been regularly monitored by the survey. For example, the 2003 year-class which was abundant at age one was almost completely absent from the survey at age two (Figure 5). The same can be mentioned for the 1999 year-class between ages four and five, and the 1982 year-class which increased significantly between these same age groups. However, the importance of this year-class declined rapidly between ages six and seven.

Instantaneous rates of total mortality do not really show any trend for the groups $1^{+}$and $2^{+}$ (Figure 6A). However, higher values were measured in the mid 1970s and the beginning and the end of the 1980s for age groups $2^{+}$and older (Figures 6B, 6C, 6D and 6E). For these same age groups, the instantaneous rates of total mortality have been increasing since the mid1990s, as with the Sinclair Z that have reached, since 2000, values greater than the unit for
ages 4-8 and blocks of four years (except 2005) (Figure 7A) and blocks of five years (Figure 8A). Slightly lower values are observed for ages 3-7 (Figures 7B, 8B) and ages 2-6 (Figures 7C, 8 C ).

## XSA: Formulations and Diagnostics

## Run 1

The first formulation used had the following characteristics: (1) catchability at age seven is assigned to ages eight and nine, and (2) catchability independent of abundance for all age groups (Table 3). This formulation presented high and negative residuals for 1989, 1990 and 2004 (Figures 9A, 9B). No age effect was observed (Figure 9C) but the standard errors of catchability were all above 0.5 (Table 3) indicating a problem in the quality of the index. A slope significantly different from the unit was measured for age five (Table 3).

## Run 2

For the second formulation, catchability was considered to be dependent on abundance for age groups one and two, and the value measured at age seven was assigned to ages eight and nine (Table 4). Adjustment problems were also observed for 1989, 1990 and 2004 (Figures 10A, 10B). There was no year effect (Figure 10C) but all the standard errors were greater than 0.5 (Table 4). A slope significantly different from the unit was measured for age seven.

These two formulations were selected given the similarity of their diagnoses. However, retrospective analysis and reference point calculations were carried out only with the second formulation for which the residual mean squared (log) was slightly lower. Because of adjustment problems, the results of these two formulations are presented for illustrative purposes only.

## XSA: Run 1

## Recruits, Mortality and Partial Recruitment

According to the recruits pattern (age one), two distinct productivity periods characterize Northwest Atlantic mackerel. The first period, between 1966 and 1974, is characterized by the presence of several consecutive strong year-classes (Table 5, Figure 11A), whereas only two strong year-classes (1982 and 1999) have been observed in the second period since 1975. Fishing mortalities gradually increased from the mid 1960s to mid 1970s (Figure 11B). Following a sharp drop in 1977, they increased in the late 1980s to stabilize between 1990 and 1995. Fishing mortalities increased very rapidly in the late 1990s and reached historic highs in the 2000s. For age groups $3-5$, a fishing mortality of 0.22 was calculated in 2000 compared to a maximum of 0.92 in 2007 (Table 5). Partial recruitment has not been constant over the years (Figure 11C).

## Abundance, Biomass and Fishing Mortality

Three periods of higher abundances were observed over the years; in the 1970s, the mid 1980s and early 2000s (Figures 12A, 12B). These periods are associated with the presence of strong year-classes. Spawning stock biomass has declined steadily since 2002, from 346,236 to a historic low of $102,457 \mathrm{t}$ in 2008 (Table 5). The highest recruitment rates were observed in 1967, 1982 and 1999 (Figure 12C).

## Stock/Fishing Mortality-Recruitment

With the exception of the 1966, 1982 and 1999 year-classes, all other strong year-classes appeared when the spawning stock biomass was high and above 700,000 t (Figure 13A). Associated with a decrease in biomass, fishing mortalities increased between 1972 and 1976 (Figure 13B). They were relatively low thereafter except in the late 1990s and 2000s.

## XSA: Run 2

## Recruits, Mortality and Partial Recruitment

Recruits are generally similar to those produced by the first formulation (Table 5, Figures 11A, 14A). Both formulations produced similar results with regard to fishing mortalities (Figures 11B, 14B) and partial recruitment (Figures 11C, 14C).

## Abundance, Biomass and Fishing Mortality

Annual abundance patterns (Figure 15A), spawning stock biomass (Figure 15B) and recruitment rates (Figure 15C) are all similar to those obtained with the first formulation.

## Stock/Fishing Mortality-Recruitment

The relationships between recruitment (Figure 16A), fishing mortality (Figure 16B) and spawning stock biomass are also similar to those produced by the first formulation. Every strong year-class, except for 1966, 1982 and 1999, appeared when the spawning stock biomass was high and above 700,000 t. Fishing mortalities increased between 1972 and 1976 and they were relatively low thereafter except in the late 1990s and mid 2000s.

## Retrospective Pattern

Recruits (age one) do not show any retrospective pattern (Figure 17A). In terms of differences, positive deviations were measured in 2004, 2005 and 2006 (Figure 17B) and a negative deviation for the relative differences in 2007 (Figure 17C) which resulted in a positive value of the Mohn statistic (average and total values) (Table 6). There is no retrospective pattern for abundance ( $1^{+}$) (Figure 18A) and positive deviations were measured for the differences between 2004 and 2007 (Figure 18B) and negative deviations for the relative differences between 2000 and 2003 (Figure 18C) for a negative value of the Mohn statistic (Table 6). Fishing mortalities show a slight retrospective pattern (Figure 19A) with negative deviations for the differences between 2004 and 2007 (Figure 18B) and positive deviations for the relative differences in 2000 and 2002 (Figure 18C) which resulted in a negative value of the Mohn statistic (Table 6).

## Reference Points

The MSY and SSB $_{\text {msy }}$ reference points obtained stochastically totalled 94,553 t and 431,020 t respectively (Figures 20A, 20B) and the corresponding total biomass was 603,726t (Figure 20C). Reference points associated with fishing mortality, calculated by yield per recruit analysis (input data, Table 7) were estimated at 0.258 for $F_{0.1}, 0.819$ for $F_{\max }$ and 0.217 for $F$ at $40 \%$ (Table 8, Figure 21). MSY and SSB $_{\text {msy }}$ reference points obtained analytically were $96,517 \mathrm{t}$ and 440,021 t respectively (Table 9).

## Stock Status for 2008

The relationship between fishing mortality (age 3-5) in the last year (2008) and $F_{\text {msy }}$ was estimated at 3.284 (Table 9). The relationship between spawning stock biomass in 2008 and $\mathrm{SSB}_{\text {msy }}$ was estimated at 0.235 for the analytical assessment and at 0.240 for the stochastic assessment.

According to these values, the status of Northwest Atlantic mackerel in 2008 was in the "overfishing/overfished" zone of the strategic management framework used by the Northeast Fisheries Science Center (Figure 22).

## Catchability

Catchability at age has increased over the years (Figures 23A, 23B). The most significant increase was measured for age groups 1 and 2.

## CONCLUSION

Given the adjustment problems encountered with XSA, the absolute values of recruitment, abundance, spawning stock biomass and fishing mortality must be interpreted with caution. These problems could be explained by a conflict between the survey data and those from the commercial fishery. Catch at age was very likely underestimated, at least on the Canadian side where catches from recreational and bait fishing are not recorded. The survey abundance index shows changes in catchability. Catches in recent years have been made up essentially of younger fish, which could be the result of an actual decline in the abundance of older fish and/or the presence of these older fish in areas not sampled by the survey.

The results obtained by XSA are quite similar to those by separable VPA, traditional VPA and iterative cohort (Grégoire and Maguire 2011). Among these methods, there is very little difference in the estimates of recruits (Figure 24A), fishing mortality (Figure 24B), abundance (Figure 24C) and spawning stock biomass (Figure 24D). This similarity is difficult to explain given that all these methods, unlike XSA, were produced without the use of an abundance index. Moreover, contrary to expectation, when the older fish are excluded from XSA (Table 10), higher abundances occurred (Tables 5, 11). All these results suggest that we should explore other methods of calculation and/or use of new abundance indices.

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Table 1. Standardized stratified mean catch per set in numbers and weight (kg) for Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008*.

| YEAR | SPRING SURVEY BACKTRANSFORMED GEOMETRIC MEAN |  |
| :---: | :---: | :---: |
|  | No/Set | Wt/Set |
| 1968 | 17.921 | 1.831 |
| 1969 | 0.190 | 0.033 |
| 1970 | 2.908 | 0.972 |
| 1971 | 3.154 | 1.023 |
| 1972 | 2.566 | 0.657 |
| 1973 | 3.490 | 0.885 |
| 1974 | 3.444 | 0.866 |
| 1975 | 1.200 | 0.232 |
| 1976 | 1.353 | 0.345 |
| 1977 | 0.535 | 0.209 |
| 1978 | 1.068 | 0.482 |
| 1979 | 0.405 | 0.231 |
| 1980 | 0.797 | 0.368 |
| 1981 | 4.606 | 1.978 |
| 1982 | 1.112 | 0.396 |
| 1983 | 0.611 | 0.121 |
| 1984 | 2.819 | 0.971 |
| 1985 | 3.036 | 1.005 |
| 1986 | 1.334 | 0.484 |
| 1987 | 14.006 | 3.676 |
| 1988 | 7.095 | 2.469 |
| 1989 | 4.321 | 0.713 |
| 1990 | 4.104 | 0.883 |
| 1991 | 6.577 | 1.477 |
| 1992 | 12.719 | 2.267 |
| 1993 | 9.767 | 2.674 |
| 1994 | 15.604 | 3.045 |
| 1995 | 15.668 | 2.865 |
| 1996 | 15.555 | 2.669 |
| 1997 | 6.679 | 1.248 |
| 1998 | 13.389 | 1.736 |
| 1999 | 24.723 | 3.723 |
| 2000 | 30.193 | 3.446 |
| 2001 | 59.106 | 6.022 |
| 2002 | 11.387 | 2.615 |
| 2003 | 44.151 | 5.177 |
| 2004 | 32.741 | 3.063 |
| 2005 | 7.761 | 1.611 |
| 2006 | 38.982 | 4.917 |
| 2007 | 15.602 | 2.606 |
| 2008 | 9.166 | 1.893 |

[^0]Table 2. Standardized stratified mean catch per set at age (numbers) of Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008*.

| AGE (yr) |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| YEAR | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10+ |
| 1968 | 12.94** | 0.4150 | 0.1890 | 0.0520 | 0.0160 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | 0.0000 |
| 1969 | 0.0300 | 0.1420 | 0.0170 | 0.0060 | 0.0000 | 0.0010 | 0.0010 | 0.0010 | 0.0000 | $\underline{0.0000}$ |
| 1970 | 0.2800 | 0.1850 | 1.3910 | 0.6120 | 0.1810 | 0.0620 | 0.0550 | 0.0880 | 0.0830 | 0.0470 |
| 1971 | 0.3280 | 0.9410 | 0.4380 | 1.1250 | 0.3930 | 0.0620 | 0.0140 | 0.0070 | 0.0060 | 0.0080 |
| 1972 | 0.8720 | 0.3080 | 0.5930 | 0.2260 | 0.3250 | 0.0580 | 0.0110 | 0.0010 | 0.0020 | 0.0000 |
| 1973 | 0.3510 | 0.3400 | 0.1760 | 0.2340 | 0.1260 | 0.2850 | 0.1820 | 0.1520 | 0.0460 | 0.1020 |
| 1974 | 0.3480 | 0.1800 | 0.2360 | 0.0480 | 0.0990 | 0.0600 | 0.2080 | 0.0910 | 0.0590 | 0.0230 |
| 1975 | 0.6540 | 0.2300 | 0.0410 | 0.0230 | 0.0060 | 0.0070 | 0.0040 | 0.0040 | 0.0030 | 0.0000 |
| 1976 | 0.0960 | 0.3870 | 0.0710 | 0.0140 | 0.0020 | 0.0010 | 0.0030 | 0.0000 | 0.0020 | 0.0010 |
| 1977 | 0.0100 | 0.0470 | 0.0850 | 0.0450 | 0.0150 | 0.0050 | 0.0030 | 0.0070 | 0.0040 | $\underline{0.0140}$ |
| 1978 | 0.0500 | 0.1100 | 0.1030 | 0.1940 | 0.0960 | 0.0280 | 0.0110 | 0.0030 | 0.0150 | 0.0180 |
| 1979 | 0.0110 | 0.0040 | 0.0070 | 0.0130 | 0.0500 | 0.0140 | 0.0100 | 0.0060 | 0.0060 | 0.0480 |
| 1980 | 0.0230 | 0.1880 | 0.0070 | 0.0050 | 0.0230 | 0.0490 | 0.0110 | 0.0110 | 0.0070 | 0.0280 |
| 1981 | 0.3360 | 0.1370 | 0.4290 | 0.0480 | 0.0460 | 0.1610 | 0.4040 | 0.2300 | 0.1390 | 0.4020 |
| 1982 | 0.4320 | 0.1950 | 0.0220 | 0.0980 | 0.0180 | 0.0100 | 0.0250 | 0.0970 | 0.0440 | 0.0840 |
| 1983 | 0.2360 | 0.2870 | 0.0220 | 0.0020 | 0.0040 | 0.0010 | 0.0000 | 0.0010 | $\underline{0.0020}$ | 0.0020 |
| 1984 | 0.2600 | 1.8010 | 0.6060 | 0.0420 | 0.0050 | 0.0430 | 0.0040 | 0.0030 | 0.0160 | $\underline{0.0840}$ |
| 1985 | 0.3380 | 0.0850 | 1.8510 | 0.2350 | 0.0280 | 0.0110 | 0.0470 | 0.0030 | 0.0100 | 0.1860 |
| 1986 | 0.1300 | 0.4500 | 0.0780 | 0.5910 | 0.1180 | 0.0080 | 0.0010 | 0.0200 | 0.0000 | 0.0470 |
| 1987 | 1.4840 | 1.7950 | 0.8740 | 0.3720 | $\underline{2.9450}$ | 0.4970 | 0.1430 | 0.0160 | 0.1380 | 0.2560 |
| 1988 | 0.6340 | 0.4580 | 0.3670 | 0.3360 | 0.3750 | 1.7690 | 0.4430 | 0.0510 | 0.0480 | 0.2230 |
| 1989 | 1.5830 | 1.6410 | 0.0710 | 0.2840 | 0.0090 | 0.0110 | 0.0670 | 0.0090 | 0.0050 | 0.0180 |
| 1990 | 1.3000 | 1.3850 | 0.5010 | 0.0160 | 0.0130 | 0.0060 | 0.0000 | 0.0760 | 0.0090 | 0.0160 |
| 1991 | 1.6700 | 0.8890 | 1.4840 | 0.5370 | 0.2400 | 0.1140 | 0.0580 | 0.0000 | 0.2690 | 0.0030 |
| 1992 | 2.9790 | 2.6422 | 0.5558 | 1.1593 | 0.7247 | 0.1156 | 0.1304 | 0.0199 | 0.0488 | $\underline{0.3450}$ |
| 1993 | 1.2070 | 2.6595 | 1.0091 | 0.3813 | 1.0544 | 0.7203 | 0.1492 | 0.1330 | 0.3325 | 0.6099 |
| 1994 | 4.1386 | 1.7436 | 2.1139 | 0.8699 | 0.2815 | 0.6019 | 0.2070 | 0.0512 | 0.0105 | 0.2251 |
| 1995 | 3.1701 | 3.4871 | 0.5893 | 1.1824 | 0.7122 | 0.2848 | 0.7191 | 0.2258 | 0.0655 | 0.1310 |
| 1996 | 4.0058 | 3.2257 | 1.3258 | 0.1481 | 0.6175 | 0.4196 | 0.1927 | 0.2800 | 0.1539 | 0.1317 |
| 1997 | $\underline{2.9998}$ | 1.1619 | 0.4485 | 0.2247 | 0.0254 | 0.1244 | 0.1149 | 0.0452 | 0.0702 | 0.0066 |
| 1998 | 5.6474 | 3.1195 | 0.6787 | 0.2863 | 0.1211 | 0.0171 | 0.0867 | 0.0634 | 0.0179 | 0.0240 |
| 1999 | 4.9932 | 4.1347 | $\underline{2.9206}$ | 0.9221 | 0.4061 | 0.1784 | 0.0498 | 0.0819 | 0.0436 | 0.0145 |
| 2000 | 14.7693 | 2.4561 | 1.1156 | 0.7272 | 0.2514 | 0.1189 | 0.0500 | 0.0000 | 0.0236 | 0.0194 |
| 2001 | 12.4608 | $\underline{26.5956}$ | 1.7582 | 0.3622 | 0.2115 | 0.0375 | 0.0114 | 0.0093 | 0.0042 | 0.0012 |
| 2002 | 1.2662 | 2.9770 | 5.7418 | 0.4438 | 0.1229 | 0.0494 | 0.0192 | 0.0014 | 0.0000 | 0.0000 |
| 2003 | 9.1159 | 8.3906 | 2.9148 | 3.2997 | 0.4028 | 0.1207 | 0.0555 | 0.0000 | 0.0000 | 0.0000 |
| 2004 | $\underline{21.9188}$ | 3.0060 | 0.3165 | 0.1166 | 0.1516 | 0.0121 | 0.0020 | 0.0000 | 0.0000 | 0.0000 |
| 2005 | 1.7745 | 3.7293 | 0.9319 | 0.1697 | 0.1354 | 0.3667 | 0.0258 | 0.0050 | 0.0000 | 0.0000 |
| 2006 | 4.4389 | 9.5737 | 6.2724 | 0.6548 | 0.1372 | 0.0521 | 0.1267 | 0.0120 | 0.0000 | 0.0000 |
| 2007 | 1.9963 | 6.9564 | 1.2098 | 1.2239 | 0.1565 | 0.0135 | 0.0224 | 0.0320 | 0.0062 | 0.0000 |
| 2008 | 3.2617 | 1.6649 | 1.6213 | 0.2450 | 0.2289 | 0.0000 | 0.0000 | 0.0000 | $\underline{0.0305}$ | 0.0000 |

[^1]Table 3. Extended Survivors Analysis (XSA) formulation for Run 1: Catchability independent of stock size for all ages and independent of age for ages $\geq 7$; last true age in the catch at age is 9 ( $10^{+}$is present).

| FLEET | FIRST YEAR | LAST YEAR | $\begin{aligned} & \text { FIRST } \\ & \text { AGE } \end{aligned}$ | $\begin{gathered} \text { LAST } \\ \text { AGE } \end{gathered}$ | Alpha | Beta |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Spring Survey: | 1968 | 2008 | 1 | 9 | 0.333 | 0.417 |
| Time series weights : | Tapered time weighting applied <br> Power = 3 over 20 years |  |  |  |  |  |
| Catchability analysis : | Catchability independent of stock size for all ages Catchability independent of age for ages $>=7$ |  |  |  |  |  |
| Terminal population estimation : | Survivor es of the final <br> S.E. of the <br> Minimum s estimates deris <br> Prior weigh <br> Tuning con | shrunk or the <br> to which <br> error for from ea <br> ot applie after | wards the Idest age estimat <br> population fleet $=.300$ | ean F <br> are shr | . 500 |  |

Mean log catchability and standard error of ages with catchability independent of year class strength and constant w.r.t. time

| Run 1: | Age | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean Log q | -15.267 | -15.014 | -15.585 | -16.052 | -16.218 | -16.431 |
|  | S.E(Log q) | 0.641 | 0.733 | 0.657 | 0.628 | 0.959 | 0.894 |
|  | Age | 7 | $\mathbf{8}$ | $\mathbf{9}$ |  |  |  |
|  | Mean Log q | -16.228 | -16.228 | -16.228 |  |  |  |
|  | S.E(Log q) | 1.257 | 0.759 | 1.122 |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |

Regression statistics :
Ages with $q$ independent of year class strength and constant w.r.t. time.

| Run 1: | Age | Slope | t-value | Intercept | RSquare | No Pts | Reg s.e |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  | $\mathbf{1}$ | 1.22 | -0.709 | 15.93 | 0.50 | 20 | 0.80 |
|  | $\mathbf{2}$ | 1.73 | -1.667 | 17.22 | 0.34 | 20 | 1.18 |
|  | $\mathbf{3}$ | 1.27 | -0.859 | 16.64 | 0.51 | 20 | 0.84 |
|  | $\mathbf{4}$ | 1.14 | -0.544 | 16.77 | 0.60 | 20 | 0.74 |
|  | $\mathbf{5}$ | 3.54 | $-2.843^{\star}$ | 31.24 | 0.11 | 20 | 2.65 |
|  | $\mathbf{6}$ | 1.23 | -0.668 | 17.98 | 0.49 | 19 | 1.13 |
|  | $\mathbf{7}$ | 1.56 | -0.966 | 20.38 | 0.25 | 18 | 1.97 |
|  | $\mathbf{8}$ | 1.15 | -0.509 | 17.20 | 0.65 | 15 | 0.89 |
|  | $\mathbf{9}$ | 1.43 | -1.593 | 18.94 | 0.72 | 15 | 0.98 |
|  |  |  |  |  |  |  |  |
| Residual mean squared (log) : |  | $\mathbf{1 . 1 3}$ |  |  |  |  |  |
| *p<0.05 |  |  |  |  |  |  |  |

Table 4. Extended Survivors Analysis (XSA) formulation for Run 2: Catchability dependent on stock size for ages $<3$ and independent of age for ages $\geq 7$; last true age in the catch at age is 9 ( $10^{+}$is present).

| FLEET | FIRST YEAR | LAST YEAR | FIRST <br> AGE | LAST <br> AGE | Alpha | Beta |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Spring Survey: | 1968 | 2008 | 1 | 9 | 0.333 | 0.417 |
| Time series weights : | Tapered time weighting applied <br> Power = 3 over 20 years |  |  |  |  |  |
| Catchability analysis : | Catchability dependent on stock size for ages < 3 <br> Regression type $=P$ <br> Minimum of 5 points used for regression <br> Survivor estimates not shrunk to the population mean <br> Catchability independent of age for ages >= 7 |  |  |  |  |  |
| Terminal population estimation : | Survivor of the fin S.E. of the <br> Minimu estimate <br> Prior we Tuning | mates sh years or ean to <br> ndard er rived fro <br> g not a rged af | k towar 5 olde <br> the es <br> for pop ach fle | he mean ges <br> ates are <br> on <br> .300 | unk = . |  |

Mean log catchability and standard error of ages with catchability independent of year class strength and constant w.r.t. time

| Run 2: | Age | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Mean $\log q$ | -15.582 | -16.052 | -16.217 | -16.431 | -16.228 | -16.228 | -16.228 |
|  | S.E(Log $q)$ | 0.657 | 0.629 | 0.959 | 0.894 | 1.256 | 0.758 | 1.122 |
|  |  |  |  |  |  |  |  |  |

Regression statistics :
Ages with q dependent on year class strength

| Run 2: | Age | Slope | t -value | Intercept | RSquare | No Pts | Reg s.e |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 0.60 | -2.10 | 14.08 | 0.49 | 20 | 0.56 |
|  | 2 | 0.57 | -1.67 | 13.73 | 0.33 | 20 | 0.69 |
| Ages with q independent of year class strength and constant w.r.t. time. |  |  |  |  |  |  |  |
|  | 3 | 0.64 | -1.788 | 14.17 | 0.51 | 20 | 0.60 |
|  | 4 | 0.68 | -1.817 | 14.42 | 0.60 | 20 | 0.57 |
|  | 5 | 0.39 | -1.741 | 12.62 | 0.11 | 20 | 0.88 |
|  | 6 | 0.60 | -1.958 | 13.70 | 0.49 | 19 | 0.79 |
|  | 7 | 0.38 | -2.753* | 11.68 | 0.25 | 18 | 0.98 |
|  | 8 | 0.75 | -1.149 | 14.09 | 0.65 | 15 | 0.72 |
|  | 9 | 1.03 | 0.115 | 15.72 | 0.72 | 15 | 0.83 |
| Residual mean squared (log): * $p<0.05$ | 1.09 |  |  |  |  |  |  |

Table 5. Extended Survivors Analysis (XSA): Recruits at age 1 (thousands of fish), fishing mortality (weighted average ages 3-5) and spawning stock biomass (metric tons) calculated from the outputs of XSA Run 1 and Run 2.

| NORTHWEST ATLANTIC MACKEREL <br> - NAFO Subareas 2-6 - |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| YEAR | RECRUITS AGE 1 <br> (thousands of fish) |  | FISHING MORTALITY <br> (average ages 3-5) |  | SPAWNING STOCK BIOMASS (metric tons) |  |
|  | RUN 1 | RUN 2 | RUN 1 | RUN 2 | RUN 1 | RUN 2 |
| 1962 | 371131 | 371131 | 0.038 | 0.038 | 175878 | 175878 |
| 1963 | 198465 | 198465 | 0.066 | 0.066 | 207482 | 207482 |
| 1964 | 264301 | 264301 | 0.047 | 0.047 | 238059 | 238059 |
| 1965 | 301995 | 301995 | 0.034 | 0.034 | 272654 | 272654 |
| 1966 | 727223 | 727223 | 0.034 | 0.034 | 321062 | 321062 |
| 1967 | 1896746 | 1896746 | 0.078 | 0.078 | 393760 | 393760 |
| 1968 | 5127975 | 5127975 | 0.223 | 0.223 | 779768 | 779768 |
| 1969 | 1998853 | 1998853 | 0.182 | 0.182 | 1097396 | 1097396 |
| 1970 | 2458808 | 2458809 | 0.217 | 0.217 | 1195723 | 1195723 |
| 1971 | 1281043 | 1281043 | 0.312 | 0.312 | 1346896 | 1346897 |
| 1972 | 1415964 | 1415965 | 0.334 | 0.334 | 1455240 | 1455240 |
| 1973 | 1126161 | 1126162 | 0.484 | 0.484 | 1116250 | 1116250 |
| 1974 | 1550555 | 1550556 | 0.517 | 0.517 | 881642 | 881643 |
| 1975 | 1690570 | 1690573 | 0.472 | 0.472 | 743107 | 743107 |
| 1976 | 291108 | 291109 | 0.747 | 0.747 | 588300 | 588301 |
| 1977 | 52029 | 52030 | 0.268 | 0.268 | 438063 | 438064 |
| 1978 | 25925 | 25925 | 0.068 | 0.068 | 460508 | 460510 |
| 1979 | 171974 | 171975 | 0.075 | 0.075 | 403059 | 403060 |
| 1980 | 47299 | 47300 | 0.102 | 0.102 | 380430 | 380432 |
| 1981 | 105347 | 105348 | 0.109 | 0.109 | 301717 | 301719 |
| 1982 | 411831 | 411833 | 0.141 | 0.141 | 273569 | 273572 |
| 1983 | 2115758 | 2115782 | 0.152 | 0.152 | 332700 | 332703 |
| 1984 | 102984 | 102987 | 0.121 | 0.121 | 392369 | 392371 |
| 1985 | 137199 | 137201 | 0.117 | 0.117 | 651264 | 651271 |
| 1986 | 96351 | 96352 | 0.130 | 0.130 | 578250 | 578258 |
| 1987 | 99604 | 99605 | 0.184 | 0.184 | 467850 | 467857 |
| 1988 | 277166 | 277177 | 0.310 | 0.310 | 391047 | 391054 |
| 1989 | 461951 | 462011 | 0.276 | 0.276 | 348538 | 348549 |
| 1990 | 99823 | 99834 | 0.266 | 0.266 | 294096 | 294115 |
| 1991 | 169352 | 169362 | 0.265 | 0.265 | 294005 | 294030 |
| 1992 | 149678 | 149681 | 0.186 | 0.186 | 231132 | 231158 |
| 1993 | 26116 | 26121 | 0.149 | 0.149 | 196845 | 196867 |
| 1994 | 138003 | 138003 | 0.207 | 0.207 | 155592 | 155615 |
| 1995 | 183692 | 183692 | 0.195 | 0.195 | 136760 | 136779 |
| 1996 | 130739 | 130740 | 0.445 | 0.445 | 137836 | 137855 |
| 1997 | 183906 | 183906 | 0.399 | 0.399 | 122572 | 122587 |
| 1998 | 90877 | 90877 | 0.511 | 0.511 | 108376 | 108386 |
| 1999 | 158032 | 158031 | 0.461 | 0.461 | 91323 | 91327 |
| 2000 | 1268238 | 1268220 | 0.215 | 0.215 | 198983 | 198984 |
| 2001 | 177888 | 177888 | 0.317 | 0.317 | 331448 | 331446 |
| 2002 | 141433 | 141434 | 0.203 | 0.203 | 346236 | 346232 |
| 2003 | 358668 | 358658 | 0.326 | 0.326 | 319928 | 319924 |
| 2004 | 600679 | 599932 | 0.559 | 0.559 | 276187 | 276163 |
| 2005 | 172297 | 172347 | 0.557 | 0.557 | 230803 | 230708 |
| 2006 | 300370 | 296083 | 0.800 | 0.802 | 197265 | 196923 |
| 2007 | 100503 | 114376 | 0.915 | 0.918 | 151046 | 150226 |
| 2008 | 241682 | 246575 | 0.651 | 0.665 | 102457 | 103504 |

Table 6. Extended Survivors Analysis (XSA): Mohn's Rho statistic for recruits (age 1), population abundance, and fishing mortality (average ages 3-5) calculated from the outputs of XSA Run 2.

| TERMINAL <br> YEAR | RECRUITS <br> AGE 1 | POPULATION <br> ABUNDANCE | FISHING <br> MORTALITY (3-5) |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 2000 | -0.697 | -0.651 | 0.323 |
| 2001 | 0.278 | -0.458 | 0.076 |
| 2002 | 0.601 | -0.267 | 0.372 |
| 2003 | -0.112 | -0.091 | 0.009 |
| 2004 | 0.804 | 0.505 | -0.155 |
| 2005 | 0.811 | 0.250 | -0.195 |
| 2006 | 0.262 | 0.392 | -0.540 |
| 2007 | -0.563 | 0.108 | -0.425 |
| AVERAGE: | 0.173 | -0.026 | -0.067 |
| TOTAL | 1.383 | -0.212 | -0.537 |
|  |  |  |  |

Table 7. Input data for the yield per recruit (YPR) and projection (AGEPRO ${ }^{1}$ ) analyses. Recruits at age 1 for all year-classes ( $n=47$ ) and selectivity data (partial recruitment) are from the outputs of XSA Run 2.

| AGE | SELECTIVITY ${ }^{2}$ | NATURAL <br> MORTALITY | STOCK <br> WEIGHT $^{3}$ | CATCH <br> WEIGHT $^{4}$ | SPAWNING <br> STOCK WEIGHT | FRACTION <br> MATURE $^{5}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 0.1260 |  |  |  |  |  |
| $\mathbf{2}$ | 0.4329 | 1 | 0.118 | 0.147 | 0.118 | 0.154 |
| $\mathbf{3}$ | 0.8941 | 1 | 0.184 | 0.237 | 0.184 | 0.807 |
| $\mathbf{4}$ | 0.9973 | 1 | 0.283 | 0.337 | 0.283 | 0.986 |
| $\mathbf{5}$ | 0.9887 | 1 | 0.364 | 0.403 | 0.364 | 0.999 |
| $\mathbf{6}$ | 1.0000 | 1 | 0.435 | 0.467 | 0.435 | 1.000 |
| $\mathbf{7}$ | 0.9827 | 1 | 0.492 | 0.512 | 0.492 | 1.000 |
| $\mathbf{8}$ | 1.0000 | 1 | 0.557 | 0.589 | 0.557 | 1.000 |
| $\mathbf{9}$ | 1.0000 | 1 | 0.603 | 0.613 | 0.603 | 1.000 |
| $\mathbf{1 0}$ | 1.0000 | 1 | 0.619 | 0.604 | 0.619 | 1.000 |
|  |  | $\mathbf{1}$ | 0.650 | 0.650 | 0.650 | 1.000 |

[^2]Table 8. Yield per recruit analysis (YPR) results ( $F$ at $40 \%$ as a proxy of $F_{m s y}$ ). Selectivity data (partial recruitment) used in this analysis are from the outputs of XSA Run 2.

|  |  |  |  | PARAMETERS |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | F | Y/R | SSB/R | TB/R | Mean Age | Mean Gen. Time | Expected Spawnings |
|  | 0 | 0 | 1.752 | 2.067 | 5.517 | 8.146 | 3.075 |
| F-0 | 0.258 | 0.162 | 0.624 | 0.901 | 3.006 | 4.731 | 1.589 |
| F-0.1 | 0.819 | 0.187 | 0.236 | 0.478 | 2.040 | 3.095 | 0.716 |
| F-Max | F at 40\% | 0.217 | 0.154 | 0.701 | 0.982 | 3.185 | 5.009 |

Table 9. Biological reference points: MSY and $B_{m s y}$ as deterministic points estimated by the YPR analysis; MSY and $B_{m s y}$ were also estimated from stochastic bootstrapped projections (AGEPRO). Recruits and selectivity data (partial recruitment) used in YPR and AGEPRO are from the outputs of XSA Run 2.

| RECRUITS$\begin{gathered} \text { (average } \\ \text { 1961-2008) } \end{gathered}$ | Analytical |  | Stochastic |  | $\frac{F(3-5)_{2008} / F_{\text {msy }}}{\text { Analytical }}$ | SSB $_{2008} / \mathrm{B}_{\text {msy }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MSY (t) | $\mathrm{B}_{\text {msy }}(\mathrm{t})$ | MSY (t) | $\mathrm{B}_{\text {msy }}(\mathrm{t})$ |  | Analytical | Stochastic |
| 627919 | 96517 | 440021 | 94553 | 431020 | 3.284 | 0.235 | 0.240 |

Table 10. Extended Survivors Analysis (XSA) formulation for Run 3: Catchability independent of stock size for all ages and independent of age for ages $\geq 5$; last age in the catch at age is 6 (no $7^{+}$).

| FLEET | FIRST YEAR | LAST YEAR | FIRST AGE | LAST <br> AGE | Alpha | Beta |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Spring Survey | 1968 | 2008 | 1 | $\underline{6}$ | 0.333 | 0.417 |  |
| Time series weights : | Tapered time weighting applied <br> Power = 3 over 20 years |  |  |  |  |  |  |
| Catchability analysis : | Catchability independent of stock size for all ages Catchability independent of age for ages $>=5$ |  |  |  |  |  |  |
| Terminal population estimation : | Survivor <br> S.E. of the <br> Minimum estimates <br> Prior weig <br> Tuning co | ates shru ears or th <br> an to whic <br> dard error ed from <br> not appli ged after | towards th 5 oldest ag <br> the estima <br> populatio ch fleet = . <br> 5 iterations | mean $F$ <br> s are shru | $k=.500$ |  |  |
| Mean log catchability and standard error of ages with catchability independent of year class strength and constant w.r.t. time |  |  |  |  |  |  |  |
| Run 3: | Age <br> Mean Log q <br> S.E(Log q) | $\begin{gathered} 1 \\ -15.428 \\ 0.613 \end{gathered}$ | $\begin{gathered} \mathbf{2} \\ -15.2129 \\ 0.7456 \end{gathered}$ | $\begin{gathered} 3 \\ -15.8634 \\ 0.6255 \end{gathered}$ | $\begin{gathered} 4 \\ -16.4715 \\ 0.5928 \end{gathered}$ | $\begin{gathered} \mathbf{5} \\ -16.8652 \\ 0.8557 \end{gathered}$ | $\begin{gathered} 6 \\ -16.8652 \\ 0.9987 \end{gathered}$ |

Regression statistics :
Ages with $q$ independent of year class strength and constant w.r.t. time.

| Run 3: | Age | Slope | t-value | Intercept | RSquare | No Pts | Reg s.e |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |
|  | $\mathbf{1}$ | 1.11 | -0.383 | 15.77 | 0.53 | 20 | 0.71 |
|  | $\mathbf{2}$ | 1.72 | -1.489 | 17.41 | 0.30 | 20 | 1.22 |
|  | $\mathbf{3}$ | 1.13 | -0.437 | 16.38 | 0.53 | 20 | 0.73 |
|  | $\mathbf{4}$ | 1.04 | -0.164 | 16.67 | 0.63 | 20 | 0.65 |
|  | $\mathbf{5}$ | 2.63 | $-2.498^{*}$ | 26.65 | 0.19 | 20 | 1.85 |
|  | $\mathbf{6}$ | 1.01 | -0.030 | 17.52 | 0.62 | 19 | 0.83 |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| Residual mean squared (log) : |  |  |  |  |  |  |  |
| * $\mathbf{p}<\mathbf{0 . 0 5}$ |  |  |  |  |  |  |  |

Table 11. Extended Survivors Analysis (XSA): Recruits at age 1 (thousands of fish), fishing mortality (weighted average ages 3-5) and spawning stock biomass (metric tons) calculated from the outputs of XSA Run 3.
$\left.\begin{array}{lccc}\hline & & & \\ \hline & & \text { NORTHWST ATLANTIC MACKEREL } \\ \text { - NAFO Subareas 2-6 - }\end{array}\right]$

## NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS

(Backtransformed Geometric Mean)


Figure 1. Mean catch per set in numbers and weight (kg) for Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008.

NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS
(Size represents AREA of bubbles)


Figure 2. Mean catch per set at age (numbers) of Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008 (the strong year-classes observed in the catch at age are indicated).


Figure 3. Year-class strength of age $1(A)$ and age $2(B)$ of Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008. The horizontal lines represent three levels of abundance: low, average and high.


Figure 4. Percentage at ages 1-4 (A) and ages 1-3 (B) of Atlantic mackerel in the NEFSC spring research vessels bottom trawl surveys conducted from 1968 to 2008.


Figure 5. Comparison between NEFSC spring research vessels bottom trawl surveys indices (shifted) at age and the indices of the same year-class one year later.


Figure 5. (Continued).
A) NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS
$Z$ as $\operatorname{Ln}\left(\Sigma\right.$ age $1^{+}$at $t / \Sigma$ age $2^{+}$at $\left.t+1\right)$

B) NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS

C) NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS

Zas Ln ( $\Sigma$ age $3^{+}$at $t / \Sigma$ age $4^{+}$at +1 )


Figure 6. Estimates of instantaneous rate of total mortality (Z) derived from the NEFSC spring research vessels bottom trawl surveys fit with a 3-year moving average over the time series and blocks of ages: $A$ ) $\ln \left(\Sigma\right.$ age $1^{+}$at $t / \Sigma$ age $2^{+}$at $\left.\left.t+1\right) ; B\right) \ln \left(\Sigma\right.$ age $2^{+}$at $t / \Sigma$ age $3^{+}$at $\left.t+1\right)$; C) $\operatorname{In}\left(\Sigma\right.$ age $3^{+}$at $t / \Sigma$ age $4^{+}$at $\left.\left.t+1\right) ; D\right) \ln \left(\Sigma\right.$ age $4^{+}$at $t / \Sigma$ age $5^{+}$at $\left.t+1\right)$; and $\left.E\right) \ln \left(\Sigma\right.$ age $5^{+}$ at $t / \Sigma$ age $6^{+}$at $\left.t+1\right)$.
D) NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS

Z as $\operatorname{Ln}\left(\Sigma\right.$ age $4^{+}$at $t / \Sigma$ age $5^{+}$at $\left.t+1\right)$

E) NEFSC SPRING RESEARCH VESSELS BOTTOM TRAWL SURVEYS


Figure 6. (Continued).

## A)

Z -SINCLAIR'S METHOD-
Ages 4 to 8 included in the analysis (block of 4 years)

B)

Z -SINCLAIR'S METHOD-
Ages 3 to 7 included in the analysis (block of 4 years)

C)

Z -SINCLAIR'S METHOD.
Ages 2 to 6 included in the analysis (block of 4 years)


YEAR

Figure 7. Estimates of instantaneous rate of total mortality ( $Z$ ) derived from the NEFSC spring research vessels bottom trawl surveys and fit according to the Sinclair's method (Sinclair 1998) for blocks of 4 years and different groups of ages: A) ages 4 to 8; B) ages 3 to 7; and C) ages 2 to 6 . The horizontal lines represent $Z=1.0$.
A)

Z -SINCLAIR'S METHOD-
Ages 4 to 8 included in the analysis (block of 5 years)

B)

Z -SINCLAIR'S METHOD-
Ages 3 to 7 included in the analysis (block of 5 years)

C)

Z -SINCLAIR'S METHOD-
Ages 2 to 6 included in the analysis (block of 5 years)


Figure 8. Estimates of instantaneous rate of total mortality ( $Z$ ) derived from the NEFSC spring research vessels bottom trawl surveys and fit according to the Sinclair's method (Sinclair 1998) for blocks of 5 years and different groups of ages: A) ages 4 to 8; B) ages 3 to 7; and C) ages 2 to 6 . The horizontal lines represent $Z=1.0$.


Figure 9. Extended Survivors Analysis (XSA) diagnostics for Run 1: A) log of catchability residuals at year and age (negative values are in white); B) plotted against time (year effect); and C) plotted against age (age effect).


Figure 10. Extended Survivors Analysis (XSA) diagnostics for Run 2: A) log of catchability residuals at year and age (negative values are in white); B) plotted against time (year effect); and C) plotted against age (age effect).


Figure 11. Extended Survivors Analysis (XSA) results for Run 1: A) Recruits at age 1 (thousands of fish); B) fishing mortality (weighted by abundance); and C) partial recruitment (from fishing mortalities) for the Northwest Atlantic mackerel. The horizontal lines in A) represent three levels of recruitment: low, average and high.


Figure 12. Extended Survivors Analysis (XSA) results for Run 1: A) Population abundance (thousands of fish); B) spawning stock biomass (metric tons); and C) recruitment rate at age 1 for the Northwest Atlantic mackerel.


Figure 13. Extended Survivors Analysis (XSA) results for Run 1: A) Stock-recruitment relationship (some year-classes are indicated); and B) stock-fishing mortality relationship for the Northwest Atlantic mackerel (some years are indicated).


Figure 14. Extended Survivors Analysis (XSA) results for Run 2: A) Recruits at age 1 (thousands of fish); B) fishing mortality (weighted by abundance); and C) partial recruitment (from fishing mortalities) for the Northwest Atlantic mackerel. The horizontal lines in A) represent three levels of recruitment: low, average and high.


Figure 15. Extended Survivors Analysis (XSA) results for Run 2: A) Population abundance (thousands of fish); B) spawning stock biomass (metric tons); and C) recruitment rate at age 1 for the Northwest Atlantic mackerel.


Figure 16. Extended Survivors Analysis (XSA) results for Run 2: A) Stock-recruitment relationship (some year-classes are indicated); and B) stock-fishing mortality relationship for the Northwest Atlantic mackerel (some years are indicated).


Figure 17. Extended Survivors Analysis (XSA) results for Run 2: A) Retrospective analysis of age 1 recruitment; B) difference; and C) relative difference to the terminal year (Mohn's Rho statistic: Average $=0.173$; total $=1.383$ ).


Figure 18. Extended Survivors Analysis (XSA) results for Run 2: A) Retrospective analysis of population abundance ages $1^{+} ; B$ ) difference; and C) relative difference to the terminal year (Mohn's Rho statistic: Average $=-0.026$; total $=-0.212$ ).


Figure 19. Extended Survivors Analysis (XSA) results for Run 2: A) Retrospective analysis of fishing mortality (average ages 3-5); B) difference; and C) relative difference to the terminal year (Mohn's Rho: Average $=-0.067$; total $=-0.537$ ).

B) SPAWNING STOCK BIOMASS

C) TOTAL BIOMASS


Figure 20. Stochastic bootstrapped projections (AGEPRO) of: A) total catch (thousands of metric tons); B) spawning stock biomass (thousands of metric tons); and C) total biomass (thousands of metric tons) with $F$ at $40 \%$ as the harvest strategy. MSY and $B_{\text {msy }}$ in $A$ ) and B) are calculated as the averages of the 2020-2108 period. Data used in this analysis are from the outputs of XSA Run 2.


Figure 21. Yield- and spawning stock biomass per-recruit analyses for the Northwest Atlantic mackerel ( $F_{0.1}=0.258, F_{\max }=0.819$ and $F$ at $40 \%=0.217$ ). Data used in these analyses are from the outputs of XSA Run 2.


Figure 22. Status of 2008 fishing mortality (F) and spawning stock biomass (SSB) of the Northwest Atlantic mackerel to $F_{m s y}$ and $S S B_{\text {msy }}$. Data used in this analysis are from the outputs of XSA Run 2.


Figure 23. Coefficients of catchability calculated for blocks of $8(A)$ and $6(B)$ years.


Figure 24. Assessments of the Northwest Atlantic mackerel from Separable VPA (SVPA), traditional VPA, iterative cohort and Extended Survivors Analysis (XSA): A) recruits at age 1 (thousands of fish); B) fishing mortality (average ages 3-5); C) population abundance ages $1^{+}$ (thousands of fish); and D) spawning stock biomass (metric tons) for the 1968-2008 period.


Figure 24. (Continued).


[^0]:    * Data from G. Shepherd and J. Deroba, NEFSC, Woods Hole, pers. comm.

[^1]:    * Data from G. Shepherd and J. Deroba, NEFSC, Woods Hole, pers. comm.
    ** Bold and underlined figures represent the strong year-classes seen in the catch at age

[^2]:    ${ }^{1}$ Recruit model $=$ empirical CDF; harvest strategy $=\mathrm{F}$ at $40 \%$
    ${ }^{2}$ From Fs (3-5), average 2004-2008
    ${ }^{3}$ Rivard's method (NOAA Fisheries Toolbox 2009a), average 2004-2008
    ${ }^{4}$ Average 2004-2008
    ${ }^{5}$ Canadian data, average 2004-2008

